

### Invariant Feature Learning for Generalized Long-Tailed Classification

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eccv2022

# Introduce



(a) Long-Tailed Distribution in Real-world Images



(b) Class-wise Balanced Data and its Imbalanced Attribute Distribution

Generalized Long-Tailed classification (GLT): class-wise imbalance + attribute-wise imbalance

# Introduce



existing LT methods fail to tackle the attribute-wise imbalance:

- They rely on class-wise adjustment, while the attribute-wise traits are hidden in GLT;
- They are based on lifting the tail class boundary to welcome more samples to increase the tail accuracy, leaving the confused region of similar attributes unchanged in the feature space.

### **Problem Formulation**

Previous Assumption:  $P(y \mid x) = rac{P(x \mid y)}{P(x)} P(y) \propto P(x \mid y) P(y)$   $p_{ ext{train}}(X \mid Y) = p_{ ext{test}}(X \mid Y)$ 



 $X = (z_c, z_a)$ 

New Assumption:

 $p_{\text{train}}(z_c|Y) = p_{\text{test}}(z_c|Y)$ 

Problem Formulation:

$$\begin{split} p(Y = k | X = x) &= p(Y = k | z_c, z_a) \\ &= \frac{p(z_c, z_a | Y = k)}{p(z_c, z_a)} \cdot p(Y = k) \\ &= \frac{p(z_c | Y = k)}{p(z_c)} \cdot \underbrace{\frac{p(z_a | Y = k, z_c)}{p(z_a | z_c)}}_{attribute \ bias} \cdot \underbrace{\frac{p(Y = k)}{class \ bias}}_{class \ bias} \end{split}$$

## Introduce

#### **Attribute Bias**

- inconsistent performances within each class
  - $\frac{p(z_a = wet \mid Y = dog, z_c = fur)}{p(z_a = wet \mid z_c = fur)} < \frac{p(z_a = fluffy \mid Y = dog, z_c = fur)}{p(z_a = fluffy \mid z_c = fur)}$

 $p(Y = dog | z_c = fur, z_a = wet) < p(Y = dog | z_c = fur, z_a = fluffy)$ 









• spurious correlations

$$\frac{p(z_a = wet \mid Y = beave, z_c = fur)}{p(z_a = wet \mid z_c = fur)} >> 1$$

$$p(Y = beaver | z_c = fur, z_a = wet)$$



# Method



#### IRM(Invariant Risk Minimization)

**Definition 3.** We say that a data representation  $\Phi : \mathcal{X} \to \mathcal{H}$  elicits an invariant predictor  $w \circ \Phi$  across environments  $\mathcal{E}$  if there is a classifier  $w : \mathcal{H} \to \mathcal{Y}$  simultaneously optimal for all environments, that is,  $w \in \arg\min_{\bar{w}:\mathcal{H}\to\mathcal{Y}} R^e(\bar{w} \circ \Phi)$  for all  $e \in \mathcal{E}$ .

#### • environment construction

we use the current classification confidence of each training sample as an imbalance indicator of attributes inside the class

$$(1 - p(Y = k|z_c, z_a))^{\beta}$$

#### • optimization problem

$$\min_{\theta, w} \sum_{e \in \mathcal{E}} \sum_{i \in e} L_{cls}(f(x_i^e; \theta), y_i^e; w),$$
  
subject to  $\theta \in \arg \min_{\theta} \sum_{e \in \mathcal{E}} \sum_{i \in e} ||f(x_i^e; \theta) - C_{y_i^e}||_2$ 

$$L = L_{cls} + \alpha \cdot L_{IFL}$$
, where  $L_{IFL} = ||f(x_i^e; \theta) - C_{y_i^e}||_2$ 

• Class-wise Long Tail (CLT) Protocol

Train-GLT: class-wise LT and attribute-wise LT Test-CBL: class-wise balanced and attribute-wise LT

• Attribute-wise Long Tail (ALT) Protocol

Train-CBL: class-wise balanced and attribute-wise LT Test-GBL: class-wise balanced and attribute-wise balanced

• Generalized Long Tail (GLT) Protocol

Train-GLT: class-wise LT and attribute-wise LT Test-GBL: class-wise balanced and attribute-wise balanced



(a) Collecting an "Attribute-Wise Balanced" Test Set for ImageNet



(b) Balancing Attribute Distribution for MSCOCO-Attribute

Table 1: Evaluation of CLT and GLT Protocols on ImageNet-GLT: Accuracy (*left in each cell*) and Precision (*right in each cell*) are reported. All methods are re-implemented under the same codebase with ResNext-50 backbone

Methods		C	ass-Wise Long	fail (CLT) Prote	ocol	Generalized Long Tail (GLT) Protocol				
< Accuracy   Precision >		$Many_C$	Medium <sub>C</sub>	Few <sub>C</sub>	Overall	$Many_C$	Medium <sub>C</sub>	Few <sub>C</sub>	Overall	
	Baseline	59.34 39.08	36.95 52.87	14.39 56.65	42.52 47.92	50.98 32.90	28.49 44.72	10.28 49.11	34.75 40.65	
	cRT [22]	56.55 45.79	42.89 46.23	26.67 41.47	45.92 45.34	48.02   38.40	34.16 38.07	19.92 33.50	37.57 37.51	
	LWS [22]	55.38 46.67	43.91 46.87	30.11 40.92	46.43 45.90	47.15 39.16	34.88 38.68	22.56 32.88	37.94 38.01	
	Deconfound-TDE [55]	54.94   49.27	43.18 43.91	28.64 33.40	45.70 44.48	46.87   42.39	34.43   35.77	22.11 26.30	37.56 37.00	
ce	BLSoftmax [46]	55.60 48.19	42.74 47.27	28.79 38.14	45.79 46.27	47.15 40.89	33.48 39.11	21.10 27.50	37.09 38.08	
an	Logit-Adj [37]	54.55 49.70	44.40 45.05	31.53 36.04	46.53 45.56	45.94   41.97	35.15 36.63	24.07 28.59	37.80 37.56	
Dal	BBN [78]	61.64 42.74	43.80 54.44	13.94   55.12	46.46 49.86	52.41   35.58	34.31 46.38	10.06 44.43	37.91 41.77	
e-l	LDAM [7]	59.05   45.39	43.23 48.80	24.44 44.99	46.74 46.86	51.02   38.78	34.13 40.39	18.46 35.91	38.54 39.08	
R	(ours) Baseline + IFL	<b>62.71</b>   42.98	40.10   56.83	18.92   <b>61.92</b>	45.97 52.06	<b>54.09</b>   36.74	31.73 49.03	13.62 51.42	37.96 44.47	
	(ours) cRT + IFL	61.27   45.84	43.96 51.67	24.32   53.64	47.94 49.63	52.75   39.11	35.14   43.36	17.92   43.35	39.60 41.65	
	(ours) LWS + IFL	61.50 45.43	43.79 52.85	23.86 55.58	47.89 50.29	53.21 38.92	34.99 44.44	17.42 45.90	39.64 42.45	
	(ours) BLSoftmax + IFL	58.00   53.70	44.70 51.73	33.49 37.58	48.34 50.39	49.92   46.86	36.11 44.31	25.71 32.01	40.08 43.48	
	(ours) Logit-Adj + IFL	56.96   56.22	46.54   50.10	36.88 33.29	<b>49.26</b> 50.02	48.25   <b>49.17</b>	37.50 41.65	29.00 25.77	<b>40.52</b> 42.28	
nt	Mixup [73]	59.68 37.96	30.83 55.74	7.09 34.33	38.81 45.41	51.04 31.85	23.10 47.25	4.94 22.88	31.55 37.44	
me	RandAug [11]	64.96 42.63	40.30 59.10	15.20 56.60	46.40 52.13	56.36 35.97	31.43 51.13	10.36 48.92	38.24 44.74	
lân	(ours) Mixup + IFL	67.71 47.77	45.87 62.58	24.71 67.77	51.43 57.44	59.36 40.95	36.77 54.67	18.06 55.10	43.00 49.25	
A	(ours) RandAug + IFL	69.35 49.42	48.05 63.19	<b>26.92</b>   66.04	53.40 58.11	60.79 42.41	39.07   55.15	20.04 57.90	44.90 50.47	
nsemble	TADE [74]	58.44 56.38	48.01 51.41	<b>36.60</b> 41.08	50.47 51.85	50.29 49.25	38.74 43.74	<b>27.99</b> 31.75	41.75 44.15	
	RIDE [61]	64.04   51.91	48.66 53.21	30.44   46.25	52.08 51.65	55.47   44.55	38.65 44.26	22.80 37.26	43.00 43.32	
	(ours) TADE + IFL	61.71   55.59	48.87 53.42	34.02 40.93	51.78 52.41	53.75   48.73	39.90 45.28	26.77 35.34	43.47 45.17	
E	(ours) RIDE + IFL	<b>65.68</b> 54.13	50.82 56.22	31.91 52.10	53.93 54.76	<b>57.84</b>   47.00	41.80 48.65	24.63 42.96	45.64 47.14	

_	Methods	Attribute-Wise Long Tail (ALT) Protocol								
<	Accuracy   Precision >	Many <sub>A</sub>		Medium <sub>A</sub>		FewA		Overall		
	Baseline	56.95	55.83	40.11	39.17	28.12	28.16	41.73	41.74	
	cRT [22]	57.45	56.28	39.72	38.65	27.58	27.35	41.59	41.43	
	LWS [22]	56.95	55.85	40.11	39.30	28.03	27.98	41.70	41.71	
	Deconfound-TDE [55]	57.10	56.58	39.80	40.08	27.29	27.96	41.40	42.36	
DCe	BLSoftmax [46]	56.48	55.56	39.81	38.96	27.64	27.60	41.32	41.37	
laı	BBN [78]	60.90	60.17	41.08	40.81	27.79	28.26	43.26	43.86	
-Pe	LDAM [7]	59.04	56.51	40.96	39.21	27.96	27.22	42.66	41.80	
Re	(ours) Baseline + IFL	61.38	60.78	44.79	44.21	31.49	31.98	45.89	46.42	
	(ours) cRT + IFL	61.12	60.25	44.26	43.65	31.02	31.31	45.47	45.81	
	(ours) LWS + IFL	61.19	60.45	44.66	44.07	31.43	31.91	45.76	46.25	
u - 1	(ours) BLSoftmax + IFL	60.19	59.46	43.54	43.14	30.85	31.46	44.86	45.43	
It	Mixup [73]	58.71	58.04	40.09	38.99	27.52	27.54	42.11	42.42	
me	RandAug [11]	62.35	61.25	45.04	44.27	31.47	31.26	46.29	46.32	
Bn	(ours) Mixup + IFL	65.90	65.88	49.43	49.43	35.40	35.89	50.24	51.04	
Y	(ours) RandAug + IFL	67.39	66.81	51.55	51.28	37.47	37.97	52.14	52.74	
Ensemble	TADE [74]	62.63	61.91	45.84	45.21	32.82	32.82	47.10	47.32	
	RIDE [61]	63.48	61.42	45.62	44.16	32.59	32.26	47.24	46.67	
	(ours) TADE + IFL	63.50	62.67	48.03	47.32	34.69	34.52	48.74	48.78	
	(ours) RIDE + IFL	67.54	67.13	51.92	51.72	37.84	38.46	52.44	53.17	

#### Table 2: Evaluation of ALT Protocol on ImageNet-GLT

Table 3: Evaluation on MSCOCO-GLT: overall performances are reported

	Protocols	CLT		GLT		ALT	
<	Accuracy   Precision >	Overall		Overall		Overall	
	Baseline	72.34	76.61	63.79	70.52	50.17	50.94
	cRT [22]	73.64	75.84	64.69	68.33	49.97	50.37
	LWS [22]	72.60	75.66	63.60	68.81	50.14	50.61
	Deconfound-TDE [55]	73.79	74.90	66.07	68.20	50.76	51.68
e	BLSoftmax [46]	72.64	75.25	64.07	68.59	49.72	50.65
anc	Logit-Adj [37]	75.50	76.88	66.17	68.35	50.17	50.94
ala	BBN [78]	73.69	77.35	64.48	70.20	51.83	51.77
e-h	LDAM [7]	75.57	77.70	67.26	70.70	55.52	56.21
¥	(ours) Baseline + IFL	74.31	78.90	65.31	72.24	52.86	53.49
	(ours) cRT + IFL	76.21	79.11	66.90	71.34	52.07	52.85
	(ours) LWS + IFL	75.98	79.18	66.55	71.49	52.07	52.90
	(ours) BLSoftmax + IFL	73.72	77.08	64.76	70.00	52.97	53.52
	(ours) Logit-Adj + IFL	77.16	79.09	67.53	70.18	52.86	53.49
ut	Mixup [73]	74.22	78.61	64.45	71.13	48.90	49.53
ne	RandAug [11]	76.81	79.88	67.71	72.73	53.69	54.71
Igu	(ours) Mixup + IFL	77.55	81.78	68.83	74.84	53.79	54.60
A	(ours) RandAug + IFL	77.71	81.10	68.16	73.97	56.62	57.12
ole	TADE [74]	76.22	78.84	66.98	71.22	54.93	55.48
m	RIDE [61]	78.29	80.33	68.59	72.20	58.90	59.43
nse	(ours) TADE + IFL	76.53	79.15	67.38	72.42	56.76	57.43
E	(ours) RIDE + IFL	78.86	80.70	69.09	72.57	58.93	59.84

Table 4: Ablation Studies on ImageNet-GLT, where overall results are reported; BLS, Focal, and IFF are balanced softmax loss [46], focal loss [31], and learning from failure [39], respectively

1	1	Ablatio	n Settings		Evaluation Protocols					
#Env	#Env Loss IFL Augment		Backbone	CLT Protocol	GLT Protocol	ALT Protocol				
1	CE	140	-	ResNext-50	42.52 47.92	34.75 40.65	41.73 41.74			
1	Focal	120	2	ResNext-50	39.93 46.99	32.52 39.12	39.58 39.85			
1	LFF	-	-	ResNext-50	41.07 45.79	33.84 38.46	40.14 40.58			
1	CE	~	-	ResNext-50	39.74 47.06	32.82 40.86	39.99 41.38			
2	IRM	-	-	ResNext-50	43.70 48.06	36.03 40.61	44.47 44.60			
2	CE	~	-	ResNext-50	45.97 52.06	37.96 44.47	45.89 46.42			
3	CE	~	<u> </u>	ResNext-50	46.06 52.81	38.32 45.55	45.95 46.43			
2	BLS	~		ResNext-50	48.34 50.39	40.08 43.48	44.86 45.43			
2	CE	~	Mixup	ResNext-50	51.43 57.44	43.00 49.25	50.24 51.04			
2	CE	~	RandAug	ResNext-50	53.40 58.11	44.90 50.47	52.14 52.74			
1	CE	-	-	RIDE-50	46.14 52.98	38.25 45.80	46.32 46.56			
2	CE	~	-	RIDE-50	49.20 54.64	41.35 47.67	48.62 48.62			
2	TADE	~	-	RIDE-50	51.78 52.41	43.47 45.17	48.74 48.78			
2	LDAM	~	-	RIDE-50	53.93 54.76	45.64 47.14	52.44 53.17			
2	LDAM	~	Mixup	RIDE-50	56.48 57.67	47.54 49.86	53.25 54.27			
2	LDAM	~	RandAug	RIDE-50	58.70 59.61	49.80 51.62	55.65 55.81			



Figure 5: (a-b) The trending of precision and accuracy after applying the IFL; (c-d) GLT baselines will automatically improve class-wise LT, while conventional LT re-balancing algorithms won't improve the attribute-wise imbalance in GLT

