



Decoupled Contrastive Learning

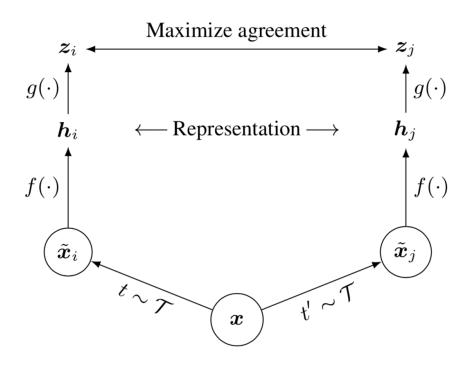
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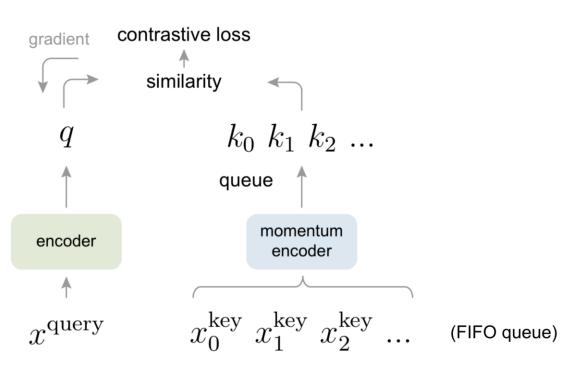
ECCV 2022

Contrastive Learning





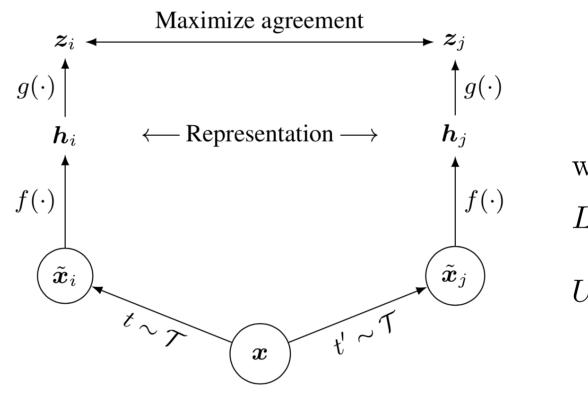
SimCLR



MoCo

SimCLR





$$L = \sum_{k \in \{1,2\}, i \in [1,N]} L_i^{(k)}$$

where

$$L_i^{(k)} = -\log \frac{\exp(\langle \mathbf{z}_i^{(1)}, \mathbf{z}_i^{(2)} \rangle / \tau)}{\exp(\langle \mathbf{z}_i^{(1)}, \mathbf{z}_i^{(2)} \rangle / \tau) + U_{i,k}}$$

$$U_{i,k} = \sum_{l \in \{1,2\}, j \in [1,N], j \neq i} \exp(\langle \mathbf{z}_i^{(k)}, \mathbf{z}_j^{(l)} \rangle / \tau)$$

Gradient



Take $L_i^{(1)}$ as an example:

$$L_{i}^{(1)} = -\log \frac{\exp(\langle \mathbf{z}_{i}^{(1)}, \mathbf{z}_{i}^{(2)} \rangle / \tau)}{\exp(\langle \mathbf{z}_{i}^{(1)}, \mathbf{z}_{i}^{(2)} \rangle / \tau) + U_{i,1}}$$

$$U_{i,1} = \sum_{l \in \{1,2\}, j \in [1,N], j \neq i} \exp(\langle \mathbf{z}_{i}^{(1)}, \mathbf{z}_{j}^{(l)} \rangle / \tau)$$

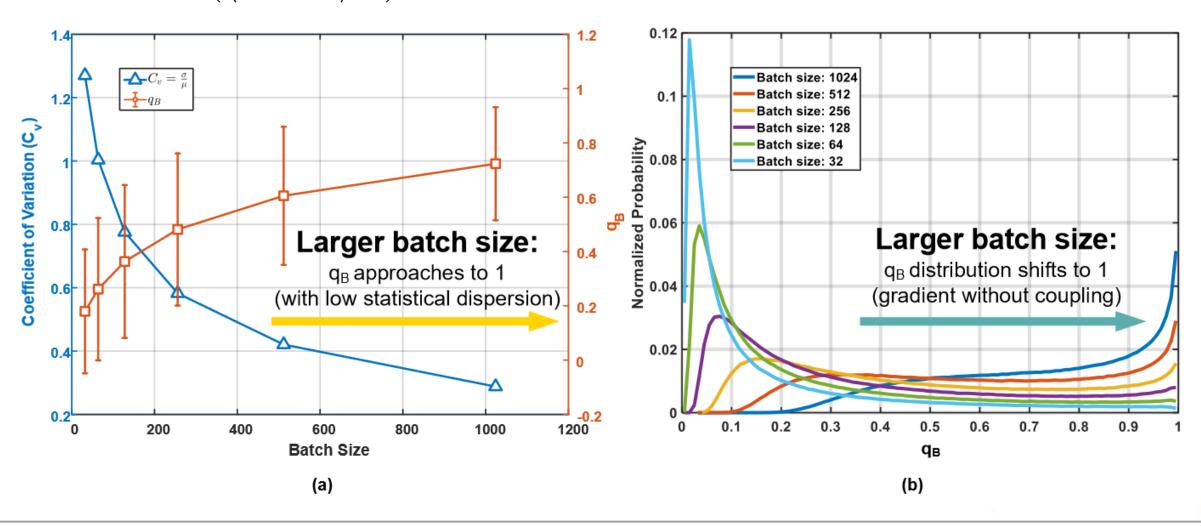
$$\begin{cases} -\nabla_{\mathbf{z}_{i}^{(1)}} L_{i}^{(1)} = \frac{q_{B,i}^{(1)}}{\tau} \left(\mathbf{z}_{i}^{(2)} - \sum_{l \in \{1,2\}, j \in [1,N], j \neq i} \frac{\exp(\langle \mathbf{z}_{i}^{(1)}, \mathbf{z}_{j}^{(l)} \rangle / \tau}{U_{i,1}} \cdot \mathbf{z}_{j}^{(l)} \right) \\ -\nabla_{\mathbf{z}_{i}^{(2)}} L_{i}^{(1)} = \frac{q_{B,i}^{(1)}}{\tau} \cdot \mathbf{z}_{i}^{(1)} \\ -\nabla_{\mathbf{z}_{j}^{(l)}} L_{i}^{(1)} = -\frac{q_{B,i}^{(1)}}{\tau} \frac{\exp(\langle \mathbf{z}_{i}^{(1)}, \mathbf{z}_{j}^{(l)} \rangle / \tau}{U_{i,1}} \cdot \mathbf{z}_{i}^{(1)} \end{cases}$$

where
$$q_{B,i}^{(1)} = 1 - \frac{\exp(\langle \mathbf{z}_i^{(1)}, \mathbf{z}_i^{(2)} \rangle / \tau)}{\exp(\langle \mathbf{z}_i^{(1)}, \mathbf{z}_i^{(2)} \rangle / \tau) + U_{i,1}}$$

Gradient



$$q_{B,i}^{(1)} = 1 - \frac{\exp\left(\left\langle \mathbf{z}_i^{(1)}, \mathbf{z}_i^{(2)} \right\rangle / \tau\right)}{\exp\left(\left\langle \mathbf{z}_i^{(1)}, \mathbf{z}_i^{(2)} \right\rangle / \tau\right) + U_{i,1}}$$



Decoupled Contrastive Learning



$$L_{DC,i}^{(k)} = -\log \frac{\exp(\langle \mathbf{z}_i^{(1)}, \mathbf{z}_i^{(2)} \rangle / \tau)}{U_{i,k}} = -\langle \mathbf{z}_i^{(1)}, \mathbf{z}_i^{(2)} \rangle / \tau + \log(U_{i,k})$$

Take $L_{DC,i}^{(1)}$ as an example:

$$\begin{cases}
-\nabla_{\mathbf{z}_{i}^{(1)}} L_{DC,i}^{(1)} = \frac{1}{\tau} \left(\mathbf{z}_{i}^{(2)} - \sum_{l \in \{1,2\}, j \in [1,N], j \neq i} \frac{\exp\left\langle \mathbf{z}_{i}^{(1)}, \mathbf{z}_{j}^{(l)} \right\rangle / \tau}{U_{i,1}} \cdot \mathbf{z}_{j}^{(l)} \right) \\
-\nabla_{\mathbf{z}_{i}^{(2)}} L_{DC,i}^{(1)} = \frac{1}{\tau} \cdot \mathbf{z}_{i}^{(1)} \\
-\nabla_{\mathbf{z}_{j}^{(l)}} L_{DC,i}^{(1)} = -\frac{1}{\tau} \frac{\exp\left\langle \mathbf{z}_{i}^{(1)}, \mathbf{z}_{j}^{(l)} \right\rangle / \tau}{U_{i,1}} \cdot \mathbf{z}_{i}^{(1)}
\end{cases}$$

Decoupled Contrastive Learning with Weight



$$L_{DCW,i}^{(k)} = -\omega(\mathbf{z}_i^{(1)}, \mathbf{z}_i^{(2)}) \langle \mathbf{z}_i^{(1)}, \mathbf{z}_i^{(2)} \rangle / \tau + \log(U_{i,k})$$

We want:

1.
$$E(\omega) = 1$$

2.
$$E[\omega((\mathbf{z}_i^{(1)}, \mathbf{z}_j^{(l)}) \left\langle \mathbf{z}_i^{(1)}, \mathbf{z}_j^{(l)} \right\rangle] \approx E[\left\langle \mathbf{z}_i^{(1)}, \mathbf{z}_j^{(l)} \right\rangle]$$

3. less weight for more similar ones

The authors choose this function:

$$\omega(\mathbf{z}_i^{(1)}, \mathbf{z}_i^{(2)}) = 2 - \frac{exp(\langle \mathbf{z}_i^{(1)}, \mathbf{z}_i^{(2)} \rangle / \sigma)}{\sum_j exp(\langle \mathbf{z}_j^{(1)}, \mathbf{z}_j^{(2)} \rangle / \sigma)}$$



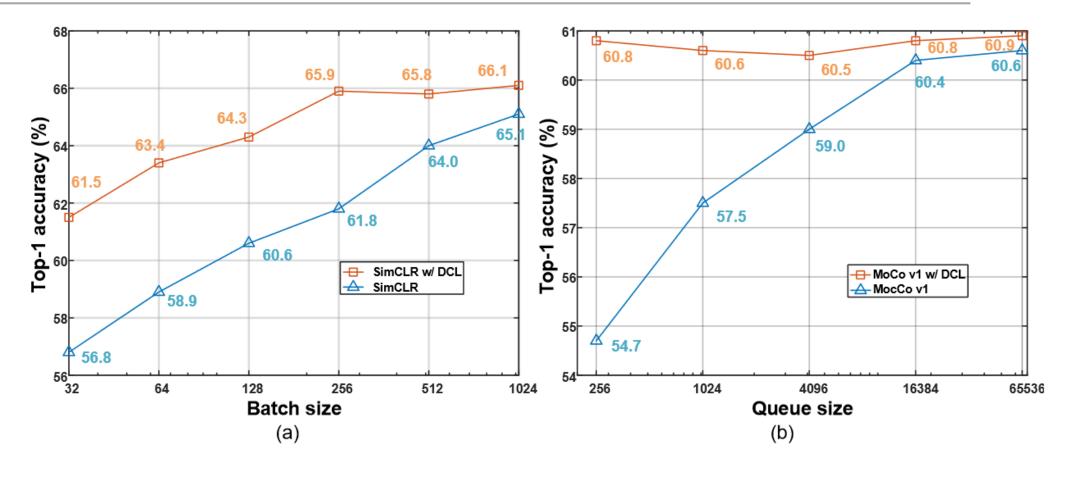


Fig. 3. Comparisons on ImageNet-1K with/without DCL under different numbers of (a): batch sizes for SimCLR and (b): queues for MoCo. Without DCL, the top-1 accuracy significantly drops when batch size (SimCLR) or queues (MoCo) becomes very small. Note that the temperature τ is 0.1 for SimCLR and 0.07 for MoCo in the comparison.



Batch Size	32	64	128	256	512	
Dataset		ImageNe	t-1K (kNN	/ Linear)		
Baseline (ResNet-50) w/ DCL (ResNet-50)	,	,	,	,	,	
Dataset		ImageNet	t-100 (kNN	/ Linear)		
Baseline (ResNet-50) w/ DCL (ResNet-50)	,	,	,	,	,	
Dataset		CIFAR	.10 (kNN /	Linear)		
Baseline (ResNet-18) w/ DCL (ResNet-18)	,	,	,	,	,	
Dataset		CIFAR	100 (kNN /	Linear)		
Baseline (ResNet-18) w/ DCL (ResNet-18)	,	,	,	,	,	
Dataset	STL10 (kNN / Linear)					
Baseline (ResNet-18) w/ DCL (ResNet-18)	,	,	,	,	,	



Table 2. Comparisons between SimCLR baseline, DCL, and DCLW. The linear and kNN top-1 (%) results indicate that DCL improves baseline performance, and DCLW further provides an extra boost. Note that results are under batch size 256 and epoch 200. All models are both trained and evaluated with the same experimental settings. The backbones are ResNet-18 and ResNet-50 for CIFAR and ImageNet, respectively.

Dataset	CIFAR10 (kNN)	CIFAR100 (kNN)	ImageNet-100 (line	ar) ImageNet-1K (linear)
SimCLR	81.4	52.0	80.7	61.8
DCL	84.2 (+2.8)	54.9 (+ 2.9)	83.1 (+ 2.4)	65.9 (+4.1)
DCLW	84.8 (+3.4)	55.2 (+ 3.2)	84.2 (+3.5)	66.9 (+5.1)



Table 4. The comparisons with/without DCL under various batch sizes from 32 to 512 on ResNet-50.

Architecture@epoch	ResNet-50@500 epoch									
Dataset		CIFA	R10 ((kNN)		(CIFAI	R100	(kNN)
Batch Size	32	64	128	256	512	32	64	128	256	512
SimCLR SimCLR w/ DCL	1	85.9 88.3				ı				

Table 5. Linear top-1 accuracy (%) comparison with MoCo-V2 on ImageNet-1K and ImageNet-100.

Queue Size	32	64	128	256	8192	64	256	65536
Dataset	Ima	ageNe	t-100	(Line	ear)	Imag	eNet-1K	(Linear)
MoCo-v2 Baseline (ResNet-50)								67.5
MoCo-v2 w/DCL (ResNet-50)	76.2	78.3	79.6	79.6	80.5	65.8	67.6	67.7



Table 6. ImageNet-1K top-1 accuracy (%) on SimCLR and MoCo-v2 with/without DCL under few training epochs. We further list results under 200 epochs for clear comparison. With DCL, the performance of SimCLR trained under 100 epochs nearly reaches its performance under 200 epochs. The MoCo-v2 with DCL also reaches higher accuracy than the baseline under 100 epochs.

	SimCLR	SimCLR w/ DCL	MoCo-v2	${ m MoCo\text{-}v2}$ w/ ${ m DCL}$
100 Epoch 200 Epoch	57.5	64.6	63.6	64.4
200 Epoch	61.8	65.9	67.5	67.7



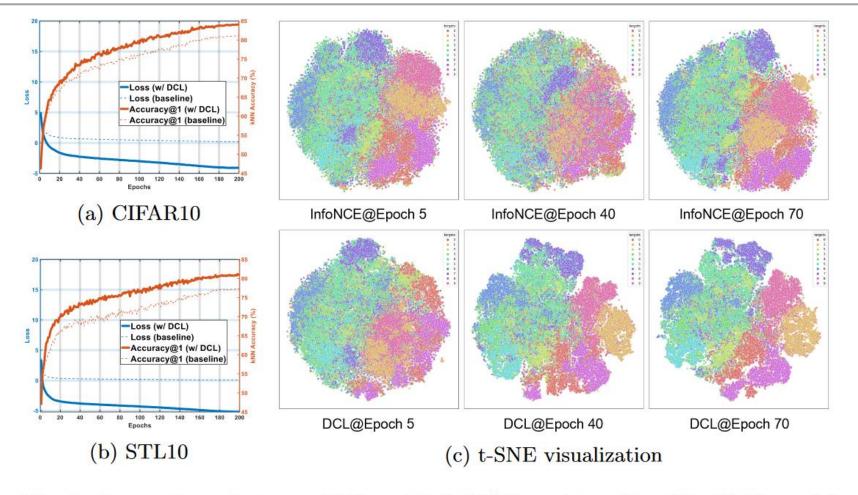


Fig. 4. Comparisons between DCL and InfoNCE-based baseline (SimCLR) on (a) CIFAR10 and (b) STL10 data. DCL speeds up the model convergence during the SSL pre-training and provides better performance than the baseline on CIFAR and STL10 data. (c) t-SNE visualization of CIFAR10 with 32 batch size. DCL shows a stronger separation force between the features than SimCLR.